Abstract

The complete 3D static responses of two different eight meter long wind turbine blade sections were tested. To experimentally investigate the 3D response, an advanced 3D digital optical deformation measuring system (ARAMIS 2M and 4M) was applied in this work. This system measures the full-field displacements ($u_x$, $u_y$ and $u_z$) of the blade surface. A least squares algorithm was developed, which fits a plane through each deformed cross section, and defines a single set of displacements and rotations (three displacements and rotations) per cross section. This least squares algorithm was also used to accommodate problems with a flexible boundary condition by determining the displacements and rotations for a cross section near the boundary. These displacements and rotations are subtracted from all other cross sections along the blade and thereby making the blade section fully fixed at the chosen cross section near the boundary.

1 Introduction

Modern wind turbine blades are constructed using a combination of different materials. Typically glass fiber reinforced plastic is used for most of the structure, with most of the fibers in the longitudinal direction to limit tip deflections.

As wind turbines increase in size the torsional eigenfrequency becomes lower and the torsional mode may couple with some of the lower bending modes. This can lead to catastrophic collapse due to the flutter instability. For larger wind turbines it therefore becomes gradually more important to be able to make reliable prediction of the torsional behavior of the blade and to calculate any structural couplings that may exist, such as the bend-twist coupling. However, correct modeling of torsional stiffness and bend-twist couplings based on FEM is subjected to some uncertainties, when numerical results are compared with experimental modal analyses of blades. In [1] the response of a shell finite element (FE) model was compared with a number of measured modal modes and the correlation related to torsional response was limited, including the 1st torsional mode and especially for the higher modes.

To investigate these uncertainties regarding the torsional stiffness and the bend-twist couplings, a number of static tests applying different load cases have been performed on a section of a full-scale wind turbine blade provided by Vestas Wind Systems A/S.

This blade section was furthermore modified by adding some additional angled UD layers on the suction and pressure side of the blade. These UD layers introduce measurable bend-twist couplings, which the original blade did not have.

The primary aim of this experimental testing was to validate a FE-model design of the two blade sections (the original and modified). The
comparison of the experimental and numerical results is used to set up guidelines for modeling wind turbine blades, which can be used to carry out reliable determination of different stiffness parameters, including the bend-twist coupling.

This paper is based on the experimental work and the analysis tools developed in [2]. The comparison between the experimental and numerical results is presented in PART II of this paper [3].

2 The test setup

A test rig was developed and used to apply five different load configurations. These configurations are adopted to capture the complete 3D response of the blade section.

Fig. 2. The test rig.

The five load configurations are the following:

- Flapwise bending
- Flapwise bending with torsion
- Edgewise bending
- Pure torsion
- Locked torsion

The fixed end of the blade section is made up of two clamps which are bolted to the steel columns of the test rig. The loads are applied at the tip end, where a movable clamp is mounted. Fig. 2 shows three hydraulic presses, but no more than two presses are used in any of the above mentioned load configurations. At the tip end a locking device is furthermore mounted which can be used to force the movable clamp to be rotated about a given point.

To ensure a sufficient transfer of the loads from the movable clamp to the blade section, the trailing edge and the spar are stiffened as shown in Fig. 3. This strengthening of the cross section is especially important for the load configurations where the cross section is twisted, as the trailing part of blade is quite flexible/soft.

Fig. 3. Close-up picture of the tip end of the blade section, where the strengthening of cross section is visible inside the spar and trailing edge.

2.1 The Five static test methods

For all five load configurations the blade is pre-bended/deformed which eliminates the effect of the mass of the movable clamp and the blade section. The measuring equipment is then tarred in the pre-bended/deformed condition. Furthermore, the blade section is only loaded in the linear-elastic regime.

In the above mentioned five load configurations only hydraulic presses equipped with spherical bearings in both ends were applied, thus reducing constraints introduced by the hydraulic presses. In the following, the five load configurations are described shortly.

2.1.1 Flapwise bending test

At the tip end, a point load is applied at the center of the spar. The center of gravity for the load clamp (movable clamp) is located at the center of the spar and the mass of the clamp will therefore not introduce at torsional moment.

The load configuration is uncomplicated to establish, since the point load is simple to introduce using a hydraulic press set-up. However, the shear force in the present load case may result in shear-extension couplings (though probably of limited size), due to the shear force.

The location of the shear center is not readily known, thus the shear-force will result in a torsional moment of an unknown magnitude (the torsional
moment is equal to the shear force multiplied with the distance to the shear center).

Fig. 4. Flapwise bending set up.

2.1.2 Flapwise bending with torsion test

This load configuration is a combination of flapwise bending and torsion. The point load is applied at a distance of 0.695 m from the center of the spar, thus introducing both a bending and torsional moment.

The load configuration is again uncomplicated to establish, and the load case may likewise result in shear-extension couplings due to the shear force. Furthermore, again the location of the shear center is not known and therefore the exact magnitude of the applied torsional moment is not known.

Fig. 5. Flapwise bending with torsion set up.

2.1.3 Pure torsion test

The pure torsion test is performed by applying two hydraulic presses creating a force couple. The two point loads are placed at a distance of 0.695 m from the center of the spar, thus resulting in a torsional moment.

This test configuration is in theory assumingly the most optimal method for determining the torsional stiffness and bend-twist couplings, due to the fact that this load configuration does not create a shear force. Furthermore, the measurement of the twist induced bending, generated by the bend-twist coupling, will be uncomplicated. However, the torsional moment is difficult to apply in practice, since the blade tip must be able to move freely, which is required in order to measure the induced bending deflections.

Fig. 7. Pure torsion set up

result in complications with regards to the boundary conditions.

The sandwich panels in the trailing part of the blade are relative soft and reaction forces in the two fixing clamps can therefore become critical. Thus, to avoid crushing of the panels, the magnitude of the edgewise point load has to be relative small, resulting in relative limited edgewise displacement, which consequently may result in measuring uncertainties.

Fig. 6. Edgewise bending set up.
2.1.4 Locked torsion test

In the locked torsion test configuration the clamp is locked in a given position which cannot move in the vertical plane. However, the clamp can rotate and translate in the horizontal plane, since the vertical steel bars, indicated in Fig. 8, are able to rotate in both ends. The movement in the horizontal plane is not entirely free since the movement is restricted to a circular arc. The point load is again applied at a distance of 0.695 m from the center of the spar, which results in a torsional moment.

Unlike the pure torsion configuration the present test configuration is uncomplicated to establish, since the blade tip is locked in a given position. Additionally, if the bend-twist couplings are of limited magnitude, the present approach is attractive in order to determine the torsional stiffness. On the other hand, if the flapwise bend-twist coupling is of a considerable magnitude, the blade tip will attempt to move in the vertical plan. However, the applied locking-system will restrict such a movement, resulting in an induced reaction force to be absorbed in the two steel bars, thus complicating the analysis.

Since the surfaces of the blade section are of a considerable size, the random speckle pattern could not be created by simply spraying small dots of black paint on the surface using an aerosol can. A harsher pattern was needed, and the best result was obtained by applying dim black spots of a size around 6 x 6 mm on the surface using a specially designed tool, which can be seen in Fig. 9.

In order for the optical system to capture as much of the blade surface as possible, the two cameras had to be positioned pointing downwards on the blade surface. The arrangement can likewise be seen in Fig. 9.

2.2 Experimental measuring method

An advanced 3D digital optical deformation measuring system (ARAMIS 2M and 4M) was applied in this work. The system records the surface of an object throughout the entire load history using two CCD cameras. The digital images are used to measure the full-field 3D displacements and surface strains of the object by digital image processing. As an aid for the digital image processing, a speckle pattern (typically black spray paint on a white background) has to be applied to the surface of the object. As the system measures a full-field displacements and surface strains, the system is highly suitable for validating FE calculations.
Furthermore, the cameras were not capable of spanning the entire 6 m cantilever blade part and the blade section was therefore divided into four measuring areas. One of these measuring areas is presented in Fig. 10.

The forces from the hydraulic presses were obtained from a digital signal from the hydraulic pump station, which was loaded into the deformation measuring system. The pressure/force signals and the deformation results for the four areas were then assembled to create a complete measuring area/surface of 6 m (the entity cantilever blade section). Each measuring area/surface was divided into 3-5 cross sections from which the displacements were obtained (see Fig.10).

For each load configuration, five image sets were generated per measuring area, where images set 1 corresponds to the undeformed area, and image set 2, 3, 4 and 5 corresponds respectively to the deformed area with 25%, 50%, 75% and 100% of the maximum load.

Each load configuration was performed three times to ensure data consistency.

3 Experimental determinations of deflections and rotations

A number of cross sections along the cantilever blade section were selected for data extraction. Each of these cross sections consists of a large number of measuring points, and in order to simplify the analysis of the measured data, a least squares algorithm was applied to determine a single set of displacements and rotations (three displacements and rotations) for each cross section. The least squares algorithm was likewise applied in the FE-analysis. The procedure effectively simplifies the comparison of experimental and numerical results, as only a single set of displacements and rotations per cross section can be compared.

The least squares algorithm consists of the following three steps:

- Computation of displacements \((u_x, u_y, u_z)\)
- Computation of twist angle \((r_z)\)
- Computation of bending slopes \((r_x, r_y)\)

3.1 Cross sectional displacements \((u_x, u_y, u_z)\)

The three displacements were calculated as average values, meaning that all the relative nodal/point displacements are summed up and divided by the number of nodes/points. \((\Delta x, \Delta y, \Delta z = \text{relative displacements})\). This is illustrated in Eq. 1.

\[
\frac{\sum_{i=1}^{n} \Delta x_i}{n}, \frac{\sum_{i=1}^{n} \Delta y_i}{n}, \frac{\sum_{i=1}^{n} \Delta z_i}{n}
\]

3.2 Angle of twist \((r_z)\)

The cross sectional rotation about the z-axis (twist-angle \((r_z)\)) is determined by fitting a linear least squares regressions curve through the deformed \(x\)-coordinates and the relative displacements in the \(y\)-direction \((dy = y_{\text{deformed}} - y_{\text{undeformed}})\). The slope of the curve is then equal to the twist-angle. The curve is given as:

\[
y(x) = r_z \cdot x + c
\]
3.3 Bending slopes ($r_y$ and $r_x$)

The rotations about the x- and y-axis are determined by fitting a linear multiple regression plane through the deformed cross section given as:

$$z(x, y) = b + r_y \cdot x + r_x \cdot y$$

(4)

The two variables $x$ and $y$ describes a plane in the three-dimensional $(x,y,z)$ space. $r_y$ and $r_x$ are the rotations about the y- and x-axis and $b$ is the intersection with the z-axis. In order to make the plane correlate as close as possible to the measured points in the aggregate, the values of $r_y$, $r_x$, and $b$ that minimize the sum of the squared residuals are found. The theory of multiple regression is shown in Eq. 5.

In the plot above (Fig.12) of the flapwise bending with torsion configuration, the blue points/o’s are plotted on the multiple regression planes.

3.4 Boundary Conditions

As the test rig is not infinite rigid, the blade section is not fully clamped either. Therefore, the digital deformation measurement system was used to investigate the deformed surface of the blade section near the “clamped” end. The undeformed and deformed surfaces near the “clamped” end are plotted in Fig. 13. The load case depicted is flapwise bending with torsion test.

It can clearly be seen that there is a small displacement in the y-direction (about 0.18 mm) near the boundary (see Fig. 13), which indicates that the blade section cannot be idealized as a cantilever beam.
The experimental and numerical results can only be compared if the experimental and numerical boundary conditions are the same. The problem with the boundary conditions can be solved applying one of following procedures:

- The actual measured boundary conditions of the test rig can be reused in the numerical model by measuring the deflections of the clamps throughout the test. A similar approach was chosen in [4].

- The two clamps can be included in the FE-model, in order to get a realistic structural behavior of the clamps. In detail the plywood plates and steel profiles should be included and contact elements should be applied to model the contact between the clamps and the blade section.

- Finally, the problems with the flexible boundary conditions can be accommodated by determining the displacements and rotations for a cross section near the boundary via the least squares algorithm. These displacements and rotations are then subtracted from all other cross sections along the blade and thereby making the blade section fully fixed in the chosen cross section near the boundary.

The last method was chosen, since it is the simplest and assuming also the most precise method. The method furthermore involves only uncomplicating FE-modeling, since idealized fixed boundary conditions, where all nodal displacements and rotations are restricted, can be applied. Furthermore, the chosen method is flexible, because an arbitrary location of the fixed end can be selected from the measured cross sections along the blade section. However, for all load cases presented, the cross section at 0.5 m from the clamp was chosen, since the displacements and rotations at this distance from the boundary were well defined.

When the blade section is subjected to torsion the cross section does not remain plane unless restrained to do so. This out-of-plane displacement is known as warping, and the restraints to these deformations, such as a fully fixed end will result in an increasing torsional stiffness. By moving the fixed end 0.5 m, the boundary effect is minimized and the validity of comparison between experimental and numerical results increased.

The modified cross sectional deflections and rotations are determined according to Eq. 6, where $L_e$ is the length of the beam elements (distance between the cross sections) and $r_{x,y,z}$ and $u_{x,y,z}$ the rotations and displacements at the new fixed end (cross section 0.5 m).

$$
i = 1, ..., rows(L_e)$$

$$u_{xi} = u_{xi} - u_{x1} - r_{yi} \sum_{i=1}^{i} L_{e i}$$

$$u_{yi} = u_{yi} - u_{y1} + r_{xi} \sum_{i=1}^{i} L_{e i}, \quad u_{zi} = u_{zi} - u_{z1}$$

$$r_{xi} = r_{xi} - r_{x1}, \quad r_{yi} = r_{yi} - r_{y1}, \quad r_{zi} = r_{zi} - r_{z1}$$

The effect of moving the fixed boundary condition to a cross section 0.5 m from the geometrically fixed end can be seen in Fig. 14, where the modified blade section is subjected to the flapwise bending test with torsion. Note that the last half meter of the cantilever blade section is not considered, and the displacements and rotations are calculated as average values of the three runs.
The reason for not considering the last half meter is that this part of the blade section is affected by the load boundary conditions.

As illustrated in Fig. 14 the effect of moving the fixed boundary condition is of great importance for the deflection in the y-direction.

4 Experimental results

In the present paper only a limited part of the experimental results are presented in detail. However, the remaining results of the different test configurations will be illustrated in part II of this paper [2], where the numerical and experimental results are compared. Eleven cross sections along the cantilever blade part were selected and for each of these cross sections a single set of displacements and rotations were determined via the least squares algorithm.

4.1 Experimental results for the original blade section

As mentioned earlier, one of the primary aims of this work is to determine if the original blade section has a bend-twist coupling or not. This is achieved by analyzing the experimental results from the flapwise bending and the flapwise bending test with torsion and applying the principle of superposition.

4.1.1 Experimental results of the flapwise bending test for the original blade section.

The flapwise bending was performed with a point load of 3923 N placed 5.607 m from the cross section at 0.5 m. This results in a bending moment and a shear force distribution as described earlier. Each load case was performed 3 times (indicated as run 1, 2 and 3) to ensure data consistency.

The results from the three runs are reasonable consistent, as one can see in Fig. 15 for the displacements and rotations. The test exclusively results in nearly pure displacements in the y-direction and a rotation about the x-axis (bending slope).

As mentioned earlier, the location of the shear center is not readily known, which means that the shear force placed in the center of the spar can result in a small torsional moment. If it is assumed that the shear center is placed in the middle of the spar, then the flapwise bending configuration indicates that the bend-twist coupling is equal or close to zero, since the bending moment do not result in a twist angle (rotation about the z-axis) of the blade section.

4.1.2 Bend-twist coupling for the original blade section

By applying the principle of superposition, it is determined if the blade section has a measurable bend-twist coupling, by subtracting the results of the flapwise bending configuration from the results of the flapwise bending with torsion configuration and the result of that is pure torsion. If a bend-twist coupling exists, then the blade will twist but also bend, because of the bend-twist coupling (twist induced bending).
The response of the blade must be linear in order for the principle of superposition to be valid. It was therefore investigated whether the response of the two load configurations were indeed linear by investigating the load-displacement relation. The result of both load configurations showed that the response were indeed linear.

In Fig. 16 it can see that the section is twisting but not bending, which indicates that the bend-twist coupling is close to zero. This was also expected as most of fibers are placed in the longitudinal direction and only a very limited amount of fibers are placed off-axis, which are necessary to create a bend-twist coupling.

**4.2 Experimental results for the modified blade section**

One of the primary aims of this work was to create a FE-model capable of modeling correct bend-twist coupled behavior. The FE-response was validated by experimental static testing. The original blade section was modified with four layers of UD1200, which were laminated on the pressure and suction side of the blade to create a measurable flapwise bend-twist coupling. The additional layers were laminated as indicated in Fig. 17.

The extra layers were laminated onto the blade section by a vacuum infusion process. Furthermore, the area between the two clamps was not laminated with extra UD-layers, since only the behavior of the cantilever part of the blade section is of interest in this study. The optimal fiber angle of 25° was determined by trial and error using FEM.
4.2.1 Bend-twist coupling for the modified blade section

The principle of superposition is again applied in order to determine if the blade section has a measurable bend-twist coupling.

![Superposition (Bend-twist blade section): Pure Torsion = Flapwise bending with Torsion - Flapwise bending](image)

If it is assumed that the shear center is located in the center of the spar, it can now be concluded from the result of the superposition analysis that the pure torsional moment induces bending of the blade section. It can therefore be concluded that the bend-twist coupling is of a measurable size. The twist-induced bending is of the magnitude of 5 mm and the twist-induced bending slope (rotation about the x-axis) is about -0.003 rad at the tip end (illustrated in Fig. 19).

Fig. 19. Result of superposition for the modified blade section.

5 Conclusion

It can be concluded that the least squares algorithm developed and applied in this work was a strong tool when the experimental results were analyzed. Furthermore, it can be concluded that problems with the flexible boundary conditions were accommodated by determining the displacements and rotations for a cross section near the boundary (the cross section at 0.5 m) via the least squares algorithm. These displacements and rotations were subtracted from all other cross sections along the blade and thereby making the blade section fully fixed at the chosen cross section near the boundary.

The least squares algorithm can also be applied in the FE-analysis, which simplifies the comparison between the experimental and numerical results as only a single set of displacements and rotations has to be compared per cross section.

It is found that the original blade section did not have a measurable bend-twist coupling. As one of the primary aims of this work was to develop a FE-model capable of modeling correct bend-twist coupling behavior, the original blade section was modified. Thus, four UD layers were laminated on the pressure and suction side of the blade section to establish a measurable flapwise bend-twist coupling.

By applying the principle of superposition it was found that this modification of the blade section induced a measurable bend-twist coupling which can be exploited in the validation process of the numerical models.

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References